# **FPGA-Based Rapid Control Prototyping of** Permanent Magnet Synchronous Motor Servo Drives

Sabin Carpiuc, The MathWorks Ltd Carlos Villegas, Speedgoat GmbH

### Key Takeaways

- Experimental position control of PM synchronous motor
- Simple framework to design multi-rate motor controllers •
- Outer loop: LQR position controller with disturbance observer
- Inner loop: field-oriented control of stator currents •
- Real-time testing using multi-core CPUs and a Xilinx FPGA •
- Automatic C and VHDL code generation from Simulink
- No need to convert to fixed-point, stay in floating-point

### Abstract

The position control problem in permanent magnet synchronous machine (PMSM) drives is a challenging problem which is subject to tight time constraints and unknown disturbances. This article presents experimental validation of a cascade control structure for position control in PMSM drives. A PI-based control algorithm is used in the inner loop to control the stator currents in the rotor d-q reference frame. Then an optimal controller is synthesized in the error space of the outer loop to control the position and velocity of the PMSM. A disturbance observer is employed to estimate the load torque and parameter mismatch of the drive and a control algorithm is deployed on a real-time system with a field-programmable gate array (FPGA) board, thereby performing an experimental validation in real-time.

### Introduction

The position control problem in PMSM drives is challenging due to tight time constraints and unknown disturbances. For best results, the control in PMSM drives is usually done through field-oriented control (FOC) [3] in the rotor d-q reference frame [4]. The basic idea of FOC is to control the torque and flux in a similar manner with the DC machine. It yields a cascade control solution with two inner loops for current control and outer velocity and position control loops [5].

#### Permanent Magnet Synchronous Machine

The PMSM mathematical model in the rotor d-q reference frame is given by the following equations [4]:

$$v_{ds}(t) = R_s i_{ds}(t) + L_d \frac{i_{ds}(t)}{dt} - \omega_e(t) L_q i_{qs}(t)$$
(1a)

$$\begin{aligned} w_{qs}(t) &= R_s i_{qs}(t) + L_q \frac{i_{qs}(t)}{dt} + \omega_e(t)\lambda_m + \\ & \omega_e(t)L_d i_{ds}(t) \end{aligned} \tag{1b}$$

$$T_e(t) = \frac{3p}{2} \left( \lambda_m i_{qs}(t) + (L_d - L_q) i_{ds} i_{qs} \right) \quad (1c)$$

$$J_m \frac{\omega_m(t)}{dt} = T_e(t) - d_m \omega_m(t) - T_L(t)$$
(1d)

$$\frac{\sigma_m(t)}{dt} = \omega_m(t) \tag{1e}$$

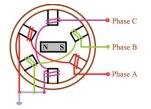


Figure - Representation of typical PM synchronous machine

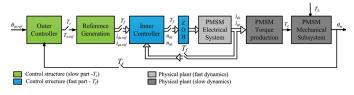
#### Challenge

For a PMSM-based servo system, synthesize a position and velocity control algorithm with the following properties: (1) fast convergence to the reference, (2) disturbance rejection and (3) low computational complexity that fits typical FPGA or microcontroller specifications.

### Control Strategy

The multi-rate cascaded control structure is depicted in the figure below and it is composed of:

1) Current control inner-loop based on field-oriented control, and 2) Position control outer-loop using a linear quadratic regulator (LQR)



#### Figure – Cascade control structure

The solution to the position tracking control problem is solved by

$$u = K(x - x_{ref}) + u_{ref}$$

with  $u_{ref}$  being related to the reference input feedforward, and x and  $x_{ref}$  being the measured and reference states of the equations of motion for the control outer-loop. The load torque is unknown but required for the input feedforward  $u_{ref}$ . A disturbance observer is derived to solve the tracking control problem.

#### **Real-Time Implementation**

A multi-rate cascade control structure is used to control the PMSM rotor position. The motor currents are controlled through the inner control loop with a faster sample rate T<sub>f</sub> while the position tracking is controlled via the outer control loop running with a slower sample rate T<sub>s</sub>. Furthermore, the PWM signal generation and incremental quadrature encoder measurements need to run at a very fast sample rate T<sub>FPGA</sub>.

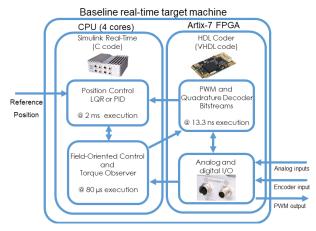


Figure – Diagram of PMSM control architecture

The load torgue estimation and the inner closed-loop is implemented with a sample time of 80  $\mu s.$  The actual rotor position is obtained from an incremental guadrature encoder fitted to the motor shaft. The controller provides a reference duty-cycle for the 3-phase PWM generator running in the FPGA.



## FPGA-Based Rapid Control Prototyping of Permanent Magnet Synchronous Motor Servo Drives

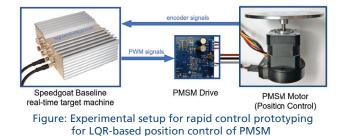
### Hardware Implementation

The cascade control structure is modeled in Simulink and deployed to a Speedgoat real-time system. The latter consists mainly of two components:

a) Baseline real-time target machine with a quad core CPU

b) IO397 Simulink-programmable FPGA I/O module with a Xilinx Artix®-7 FPGA connected to 8 analog inputs, 8 analog outputs and 14 digital I/O

Code is automatically generated from the Simulink models to the CPU or FPGA by using Simulink Real-Time<sup>™</sup> or HDL Coder<sup>™</sup>, respectively. The experimental setup is depicted on the right.



### **Experimental Results**

The tracking performance of the position control is tested with a step change of 180 degrees. The position results are shown in the figures below. The LQR controller (green solid lines) can be optimized to obtain smooth and fast transient response. When a constant disturbance is applied after around 2.1 seconds, the LQR controller (green solid lines) has a better disturbance rejection than the PID controller (red dotted lines), both for transient and steady-state conditions.

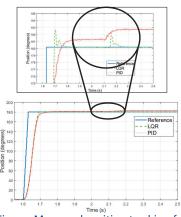
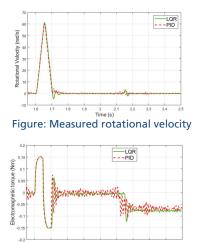
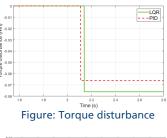


Figure: Measured position tracking for step change with torque disturbance



Zime (s)

Figure: Measured electromagnetic torque



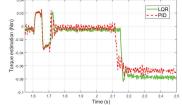


Figure: Torque estimation from observer

### Conclusion

This article discusses a **multi-rate controller architecture** to control angular position of a PMSM. An LQR position controller with a disturbance observer is derived and modelled in Simulink. A PID controller is also modelled for comparison purposes. The Simulink model of the control architecture is deployed to a Speedgoat real-time target machine with a multi-core CPU and a Xilinx FPGA, that is in turn connected to a PMSM drive and motor. With the proposed rapid control prototyping setup, the Simulink-based model could be later deployed to a microcontroller or FPGA for final production. Experimental results demonstrate the **improved disturbance rejection of the LQR controller**.

### References

[1] J. Song, N. Xi, K. J. F. Xu, and F. Zou, "Servomotor modelling and control for safe robots," in IEEE International Conference on Robotics and Biomimetics (ROBIO), 2015, pp. 1221–1226.

[2] K. Belda and D. Vo'smik, "Explicit generalized predictive control of speed and position of pmsm drives," *IEEE Transactions on Industrial Electronics*, vol. 63, no. 6, pp. 3889–3896, 2016.

[3] N. K. Adamopoulos, F. A. Karamountzou, A. G. Sarigiannidis, and A. G. Kladas, "Comparison of field oriented versus model predictive torque control techniques for monitoring interior pm traction motor over wide speed range," *in IEEE 11th International Symposium on Diagnostics for Electrical Machines, Power Electronics and Drives (SDEMPED)*, 2017, pp. 353–359.

[4] P. C. Krause, O. Wasynczuk, S. D. Sudhoff, and S. Pekarek, Analysis of Electric Machinery and Drive Systems, third. Wiley–IEEE Press, 2013.
[5] M. Tetik, Y. Ulu, and O. Gurleyen, "Off-line autotuning of a microcontroller-based pmsm servo drive," *in 2018 XIII International Conference on Electrical Machines (ICEM)*, 2018, pp. 1617–1622.

[6] M. D. S. Hasan, A. E. Hafni, and R. Kennel, "Position control of an electromagnetic actuator using model predictive control," in IEEE International Symposium on Predictive Control of Electrical Drives and Power Electronics (PRECEDE), 2017, pp. 37–41.

[7] S. Carpiuc and C. Villegas, "Real-time position control in permanent magnet synchronous machine drives," in 20th European Conference on Power Electronics and Applications (EPE'18 ECCE Europe), 2018, pp. 1–8.

[8] A. E. Bryson and Y. C. Ho, Applied Optimal Control: Optimization, Estimation, and control. Taylor and Francis Group, 1975.



### About the Authors



#### Sabin Carpiuc

Address: The MathWorks Ltd, Matrix House, Cambridge Business Park, Cambridge, United Kingdom Phone: +44-1223-428609 Email: <u>sabin.carpiuc@mathworks.co.uk</u> Website: <u>www.mathworks.com</u>

#### Short biography:

Sabin Carpiuc received the M.Sc. and Ph.D. degrees in systems engineering from the "Gheorghe Asachi" Technical University of Iasi, Iasi, Romania, in 2012, and 2015, respectively.

From March 2010 to June 2016, he was with the Powertrain Division, Business Unit Hybrid Electric Vehicle, Continental Automotive Romania, Iasi R&D Center, Iasi, Romania. From October 2010 to June 2016, he has been also an Associate Teaching Assistant with the Department of Automatic Control and Applied Informatics, the "Gheorghe Asachi" Technical University of Iasi. In June 2016, he joined the Physical Modeling group at MathWorks in Cambridge, United Kingdom.

His research interests include physical modeling, electric machines and power electronics, automotive electric traction drives, model predictive control and optimization, constrained control and automotive control systems.



#### **Carlos Villegas**

Address: Speedgoat GmbH, Waldeggstrasse 30, 3097 Liebefeld, Switzerland Phone: +41-26 670 75 50 Email: carlos.villegas@speedgoat.ch Website: www.speedgoat.com

#### Short biography:

Carlos Villegas has over 10 years of R&D experience in electrical machines, power electronics and automotive control systems, including the design, controls, and hardware-in-the-loop testing of power converters up to 2 MW.

He is inventor in 4 patents, and author of 17 technical papers. He received a Ph.D. degree in Control Engineering from the Hamilton Institute, NUI Maynooth, Ireland in 2019; an M.Sc. degree in Mechatronics from CINVESTAV, Mexico in 2004; and an M.Eng. degree in Electrical-Mechanical Engineering from Tec de Monterrey, Mexico in 2002.

As Industry Manager for Electrification at Speedgoat, he is responsible for real-time solutions for motors, power electronics, and battery systems.

